

LESSON 11

Read about this PROVISIONAL EDITION in the front matter to this book.
Check the NFB website periodically for updates to this lesson.

SIGNS OF SHAPE

- [Basic Shapes](#)
- [Shapes with Structural Modification](#)
- [Shapes with Interior Modification](#)
- [Other Details](#)
- [Calculators and Keyboards](#)
- [Icons](#)
- [Shapes Used as Signs of Omission](#)
- [Identified Signs of Shape](#)

TYPEFORMS

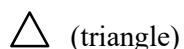
- [Labeled Mathematical Statements](#)
- [Typeform Indicators for Words/Phrases](#)

FORMAT

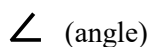
- [Displayed Material with Labels](#)
- [Labeled Mathematical Statements](#)

SIGNS OF SHAPE

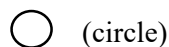
11.1 Definition: A sign of shape is a miniature picture of a geometric figure or an object.



(triangle)



(angle)



(circle)

Basic Shapes

A basic shape is represented in braille by the shape indicator followed by a numeral, one or more letters, or a dot combination suggestive of the shape.

Shape Indicator



11.2 Basic Signs of Shape Represented by Numbers—Regular Polygons: A closed figure that has equal sides and equal angles is called a *regular polygon* and is represented by the shape indicator followed by a numeral specifying the number of sides in the figure.

Square (4-sided)



Regular Pentagon (5-sided)




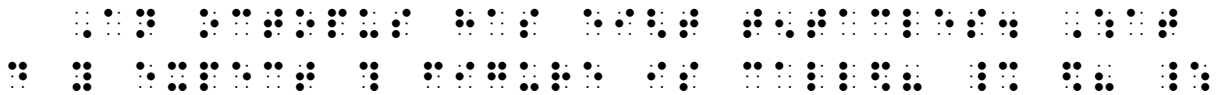
Regular Hexagon (6-sided)



Note that the equilateral triangle, which is a regular polygon, is not represented by the number three. See [11.4](#).




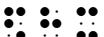


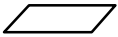









11.2.1 Unlisted Regular Polygons: Symbols which represent regular polygons with seven or more sides are not provided for in the Nemeth Code. If the unlisted shape is a *regular polygon*—that is, it is a closed figure with equal sides and equal angles—the transcriber is instructed to devise a symbol in accordance with the principles above, based on the number of sides the shape has. It may be helpful to include a tactile drawing of the shape. Unlisted regular polygon constructions do not require a transcriber's note.

Example 11.2-1 An octopus has eight tentacles. What do you expect this figure is called? 



In addition to the transcriber-devised braille symbol, the shape is presented as a tactile graphic at the first mention of this shape. Follow directives in the most recent edition of Guidelines and Standards for Tactile Graphics.

11.3 Basic Signs of Shape Represented by Letters—Irrregular Polygons: A closed figure which has at least two unequal sides and/or two unequal angles is called an *irregular polygon* and is represented by the shape indicator followed by a letter or a combination of letters suggestive of the name of the shape. (The derivation of the letter following the shape indicator is underlined in the list below.)

<u>D</u> iamond		
Irrregular <u>H</u> exagon		
Irrregular <u>P</u> entagon		
<u>P</u> arallelogram		
<u>Q</u> uadrilateral		
<u>R</u> ectangle		
<u>R</u> hombus		
<u>T</u> rapezoid		











We apologize for the blurry images in this lesson. We hope to provide better graphics in future editions.

A transcriber's note is required to define the figure unless it is described in the narrative. In your note, give the name or description of the symbol used. Include a drawing of the shape when appropriate.

Figure 10: A sequence of 1000 images showing the evolution of the system. The images are arranged in three rows: the first row contains 333 images, the second row contains 333 images, and the third row contains 334 images. The images show a complex, fractal-like structure that evolves over time, with a central region of high density and a surrounding region of lower density. The structure appears to be composed of many small, interconnected components, forming a larger, more complex shape.













11.4 Other Basic Signs of Shape Represented by Letters: The following shapes are also represented by the shape indicator followed by a letter suggestive of the name. (The derivation of the letter following the shape indicator is underlined.)

<u>C</u> ircle		
<u>E</u> llipse		
<u>I</u> ntersecting Lines		
<u>S</u> tar		
<u>T</u> riangle		

5/9/2020 revision

The following shapes were introduced in **Lesson 6** as signs of comparison. They may also be used in print to simply replace the word they represent. Notice that two signs in this category begin with the negation symbol (34) immediately followed by the shape indicator.

<u>A</u> rc, Concave Upward		
Is <u>P</u> arallel To		
Is <u>N</u> ot Parallel To		
Is <u>P</u> erpendicular To		
Is <u>N</u> ot <u>P</u> erpendicular To		

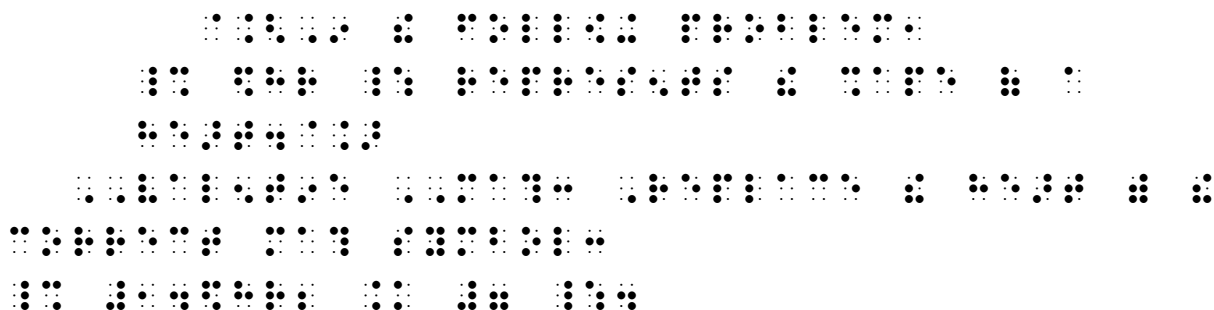
Example 11.4-1 Line AD  Line BC.





11.4.1 Other Unlisted Basic Shapes: Basic shapes not provided for in the Nemeth Code are formed in accordance with the principles above. One must be careful not to choose a symbol which already has an assigned meaning in the Nemeth Code. Refer to Appendix B of the Nemeth Code for a list of symbols already in use. Symbols beginning with dots 1246 begin on page 222; symbols beginning with dots 34 are on page 231.

A transcriber's note is required to define the figure. Give the name or description of the symbol used. Include a drawing of the shape if it is vital to the mathematical topic at hand.







Example 11.4-2 VALENTINE MATH: Replace the heart with the correct math symbol: $14 \heartsuit 2 = 7$.





The transcriber represents the heart shape with  since  means "rhombus".



Note: Refer to the most recent edition of *Guidelines and Standards for Tactile Graphics* regarding picture objects (such as counting symbols, pictographs, etc.) used in Kindergarten through third grade materials.

11.5 Basic Signs of Shape Represented by Other Dot Combinations: Three additional shapes are identified in the Nemeth Code.

Angle		
Arc, Concave Downward		
Inverted Triangle		

11.6 Filled-In and Shaded Shapes: A filled-in or shaded closed shape (circle, diamond, square, etc.) is represented as such by the filled-in shape indicator or the shaded shape indicator. The appropriate indicator is placed between the shape indicator and the shape symbol.

Filled-in shape indicator	
Shaded shape indicator	

  (filled-in star)

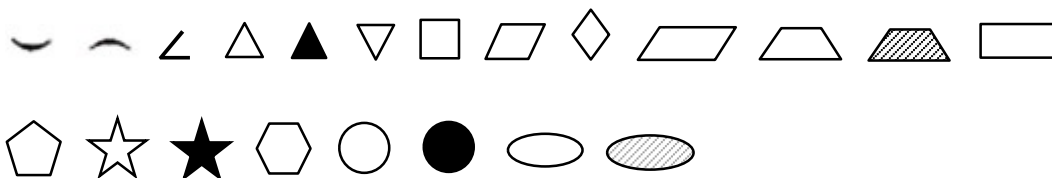
  (shaded circle)

Shapes used as icons in non-mathematical context are discussed later in this lesson. See [11.26](#).

Instructions: Leave one space between each shape. Braille as many shapes on one braille line that will fit before beginning a new line. Use "fl" to represent the flower shape and "ch" to represent the chicken. The required transcriber's note may be omitted in this practice exercise.

PRACTICE 11A

Listed Shapes




Unlisted Shapes




Shapes with Structural Modification

11.7 Definition and Construction: A shape with structural modification is one in which the general print form of a basic shape (such as *triangle*) is changed to show a more specific form (such as *right triangle*).

Basic shape: Triangle 

More specific form: Right Triangle 




Composite signs in which two or more signs of shape are combined are also structurally modified shapes, for example, two *angle* shapes in print combine to form the symbol for *adjacent angles*.




Basic shape: Angle 















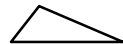













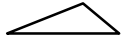






More specific form: Adjacent Angles 

A shape with structural modification is represented by

- the basic shape symbol,
- followed by the structural shape-modification indicator,
- followed by a letter or an uncontracted combination of letters suggestive of the change in the shape,
- ending with the termination indicator which signals the end of the modification.

Shape indicator	
Structural shape-modification indicator	
Termination indicator	

11.8 Structurally Modified Triangles: The following five structurally modified triangles are identified in the Nemeth Code. Each symbol starts with the basic shape symbol for "triangle"  . The derivation of the letter following the structural shape-modification indicator  is underlined in the list of modified triangles below.

<u>A</u> cute Triangle		     
<u>I</u> sosceles Triangle		     
<u>O</u> btuse Triangle		     
<u>R</u> ight Triangle		     
<u>S</u> calene Triangle		     








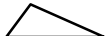

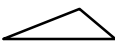

11.10 Unlisted Shapes with Structural Modification: Structurally modified shapes which are not provided for in the Nemeth Code are formed in accordance with the principles above. Review the definition of *structural modification* in [11.7](#) to properly identify the unlisted shape. Be careful not to choose a symbol which already has an assigned meaning in the Nemeth Code. Refer to Appendix B of the Nemeth Code for a list of symbols already in use. Symbols beginning with dots 1246 begin on page 222.

Explain the unlisted shape in a transcriber's note, giving the name or description of the symbol used. Include a drawing of the shape when appropriate.

Instructions: Review simple table format in **Lesson 6**. Do not braille tables side-by-side. After completing the "Angle/Symbol" table, leave one blank line and then begin the "Triangle/Symbol" table. Do not use box lines.

PRACTICE 11B

Structurally Modified Shapes

<u>Angle</u>	<u>Symbol</u>		<u>Triangle</u>	<u>Symbol</u>
right			isosceles	
straight			right	
obtuse			acute	
complementary			obtuse	
supplementary			scalene	
vertical				

Shapes with Interior Modification

11.11 Definition and Construction: A shape with interior modification is a basic shape (for example, a *circle*) within which a letter, a numeral, a sign of operation, or other sign appears.




Basic shape: Circle ○

More specific form: Circle with number 8 inside ⑧

More specific form: Circle with asterisk inside 















A shape with interior modification is represented by









- the basic shape symbol,
- followed by the interior shape-modification indicator,
- followed by the symbol corresponding to the interior sign,
- ending with the termination indicator which signals the end of the modification.



Shape indicator	
Interior shape-modification indicator	
Termination indicator	







Note: Symbols, numbers, words, etc. that represent keys on a calculator or a keyboard follow rules for keystrokes. See [11.23](#).


11.12 Circles with Interior Modification: Eleven circles with interior modification are identified in the Nemeth Code. Each symbol starts with the basic shape symbol for "circle" ⠠⠨⠠⠨ followed by the interior shape-modification indicator ⠠⠨⠠⠨. Notice that an interior numeral includes a numeric indicator and that the contracted form of the right-pointing arrow is not used.




Circle with Interior Arrow Pointing Right		
Circle with Interior Arrow Pointing Left		
Circle with Interior Arrow Pointing Up		
Circle with Interior Arrow Pointing Down		
Circle with Interior Capitalized Letter		
Circle with Interior Numeral		
Circle with Interior Cross		

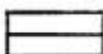











Circle with Interior Dot		
Circle with Interior Minus Sign		
Circle with Interior Plus Sign		
Circle with Interior Vertical Bar		





11.13 Angles with Interior Modification: Three angles with interior modification are identified in the Nemeth Code. Each symbol starts with the basic shape symbol for "angle"  followed by the interior shape-modification indicator .

Angle with Interior Arc		
Angle with Interior Clockwise Arrow		
Angle with Interior Counterclockwise Arrow		

Note: When the print copy uses the "angle with interior arc" symbol throughout the text to simply mean "angle", the simple braille shape symbol for "angle"  may be used. A transcriber's note is required to inform the reader of the substitution.







11.14 Rectangles and Squares with Interior Modification: One rectangle and seven squares with interior modification are identified in the Nemeth Code. Each symbol starts with the basic shape symbol for "rectangle"  or for "square"  followed by the interior shape-modification indicator .

Rectangle with Interior Horizontal Bar		
Square with Interior Bar		
Interior Horizontal Bar		
Interior Vertical Bar		
Square with Interior Diagonal		
from Lower-Left to Upper-Right		
from Upper-Left to Lower-Right		
Square with Interior Diagonals		





Square with Interior Dot		
Square with Interior Numeral		

11.15 Words Enclosed in Shapes: Words enclosed in shapes are transcribed according to the methods for shapes with internal modification and must be enclosed within Nemeth switches. *Note: Words that represent keys on a calculator or a keyboard follow rules for keystrokes. See [11.23](#).*







11.16 Two or More Vertically Arranged Modifiers: When two or more vertically arranged symbols occur within a basic sign of shape, the basic shape symbol and the interior shape-modification indicator are followed first by the symbol for the upper and then by the symbol for the lower interior sign. The termination indicator is used only after the last symbol.

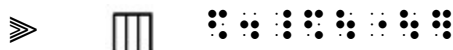
Circle with Interior Arrow Pointing Right		
Over Interior Arrow Pointing Left		
Circle with Interior Arrow Pointing Left		
Over Interior Arrow Pointing Right		

11.17 Two or More Horizontally Arranged Modifiers: When two or more horizontally arranged symbols occur within a basic sign of shape, a multipurpose indicator (dot 5) is inserted between the interior modifiers to show that they are printed horizontally, not vertically. The termination indicator is used only after the last symbol.

Circle with Interior Arrow Pointing Up		
Followed by Interior Arrow		
Pointing Down		
Circle with Interior Arrow Pointing Down		
Followed by Interior Arrow		
Pointing Up		

11.18 Unlisted Shapes with Interior Modification: Shapes with interior modification not provided for in the Nemeth Code are formed in accordance with the principles for the construction of such shapes. Review the definition of *interior modification* in [11.11](#) to properly identify the unlisted shape.

»		
»		
»		





A symbol which already has an assigned meaning in the Nemeth Code must not be used for the unlisted sign of shape. If necessary, explain the shape in a transcriber's note giving the name or description of the symbol used. Include a drawing of the shape when appropriate.


Instructions: Braille this as a simple list, not as columns.


PRACTICE 11C


Squares with Interior Modification

Square with interior numeral 2 

Square with interior dot 


Square with interior horizontal bar 

Square with interior vertical bar 

Square with interior diagonals 

Other Details


11.19 Spacing with Signs of Shape: Except for keystroke constructions (see 11.24.2 below), a sign of shape is spaced in accordance with its assigned meaning. For example, operation signs are unspaced,

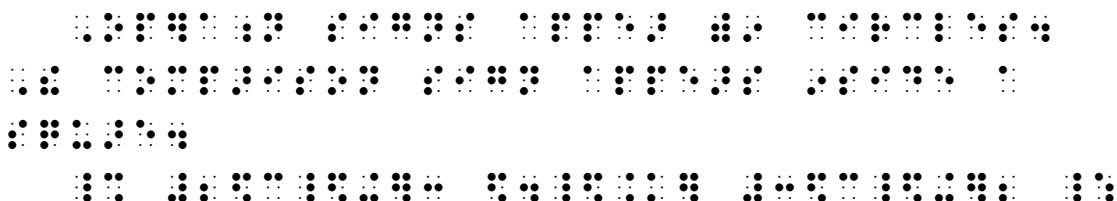
 $x \oplus y$ 

and comparison signs are spaced.

 $x \ominus y$ 

Example 11.19-1 Operation signs appear within circles. The comparison sign appears inside a square.

$2 \oplus 3$  $3 \oplus 2$



11.20 Punctuation with Signs of Shape: Signs of shape are punctuated mathematically when the

11.21 Plurals/Possessives: The uncapitalized letter "s" or the apostrophe-s combination occurring *inside or after* a sign of shape to show its plural or possessive are placed after the shape symbol in braille. Apply the general rules for the English letter indicator to the plural or possessive ending.

Example 11.21-1 \triangleleft_s and \triangle_s .

Each "s" is printed inside the shape.

Example 11.21-2 \angle s and \triangle s.

Each "s" follows the printed shape.

Example 11.21-3 \angle 's and \triangle 's.

A punctuation indicator precedes each apostrophe.

Example 11.21-4 (\angle 's, \triangle 's, and \bigcirc 's.)

Each "apostrophe-s" is punctuated mathematically because each is associated with a mathematical item.

11.22 Further Considerations Regarding Transcriber-Devised Shapes: As previously noted, when encountering a shape not provided for in the Nemeth Code the transcriber may devise a symbol if that shape appears more than occasionally. The print shape should also be drawn as a raised-line diagram the first time the new symbol is introduced. In addition to the guidelines regarding unlisted shapes throughout this lesson, observe the following.

11.22.1 Usage Rules Regarding Interior Numerals and Arrows: Transcriber-devised forms should heed the following principles regarding interior numerals and arrows.

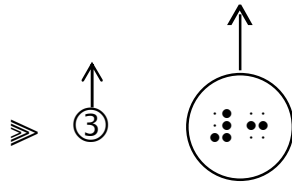
- The numeric indicator is used before a *numeral* or before a *decimal point and a numeral* following the interior shape-modification indicator.

⑧

- If a *right-pointing arrow* in regular type with a full barb and single shaft of ordinary length is part of a shape symbol, its contracted form is not used.



11.22.2 Shapes Represented by Drawing: Drawn-in shapes are often more readable than elaborate braille constructions. Since it is not possible to formulate specific rules for the selection of an appropriate form, the decision is left to the experience and judgment of the transcriber. Shapes may also be represented by a combination of drawing and braille symbols. For example, if a modified shape cannot be represented clearly by braille symbols alone, the shape can be drawn and the modification shown in braille.



PRACTICE 11D

1. $\square, \bigcirc, \triangle, \angle, \odot, \triangleleft$.
2. (\bigcirc 's, \angle 's, and \triangle 's.)
3. $a \oplus (b \oplus c)$
4. $r \otimes s \otimes ___ = rst$
5. How many \triangleleft can you find in the giant \square ?

Calculators and Keyboards

11.23 The Keystroke Indicator: When a print shape with interior modification depicts a labeled calculator or computer key, a contracted form employing a keystroke indicator is used in braille. A keystroke is represented by

- the keystroke indicator,
- followed by the label printed on the calculator key or the computer key,
- ending with the termination indicator which signals the end of the modification.

Keystroke indicator	
Termination indicator	

11.23.1 Shape in Print: The keystroke indicator is used regardless of the shape of the key in the print copy.

➤

➤

The actual key shape(s) used in a particular text should be specified on the Transcriber's Notes page. For example, "Calculator keys are depicted in print as square shapes."

11.24 Other Details Concerning Keystrokes

11.24.1 The Label: Regarding the item depicted on the key, note the following.

- Capitalization is duplicated in braille.

➤

➤

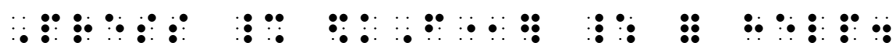
Reminder: Words are brailled without contractions.

- Follow the usual rules of the Nemeth Code for typeform and use of indicators.

➤

Italic typeform for variables is disregarded. A baseline indicator is required before brailing the termination indicator in this example because the keystroke is on the baseline of writing.

Example 11.24-1 Press  for help.



A multipurpose indicator (dot 5) is needed to show that the numeral is not a subscript. Review section 7.16.

- The numeric indicator is not required within the keystroke construction.










➤  

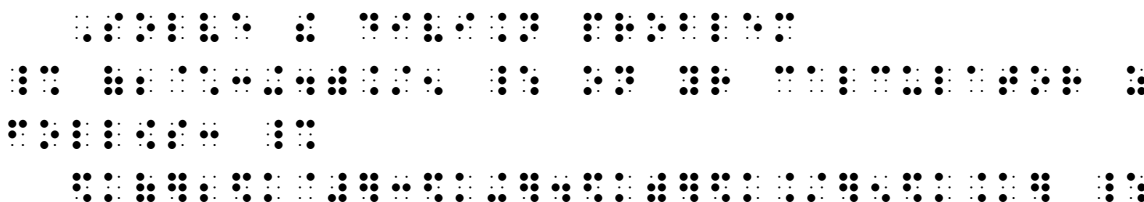
Compare to a shape with interior modification which does require a numeric indicator. See [11.22.1](#).

11.24.2 Spacing

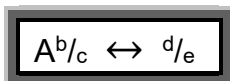
- No space is left between keystroke constructions and other similar constructions or mathematical symbols in a sequence of related calculations.

Example 11.24-2 Solve the division problem $(2 \times 3 + 4) \div 5 =$ on your calculator as follows:



- Arrows contained in the labels on the keys should not be spaced from the material to which they apply.


➤ 



➤ 



Example 11.25-1 $n \times P \times ((1 - (1 + i\%)^n)^{+/-}) \div i\%$




11.26 Consistency in Representation of Icons: When non-word UEB symbols such as icons appear in mathematical context, the symbol may be brailled in Nemeth context using the UEB transcriber-defined shape indicator \mathbb{A} . This UEB indicator may be transcribed in either UEB context or Nemeth context without the insertion of switch indicators. List the icon on the Special Symbols page.

Example 11.26-1 (Earlier in the book it is stated that a gold ribbon indicates extra credit problems.)

Evaluate each expression.

13. $\frac{1}{2}(5 + 13) - 4 \cdot 5$

14. $(5 + 11) - (24 - 15) \cdot (3)$

 15. $6^2 + 3 \cdot 7 - 9 \div 3$

The BANA Nemeth Code Technical Committee is discussing details regarding alignment of identifiers when some items are marked. The transcription of this example will be revisited after rulings are made.

Line 4: An icon was created to represent the "extra credit" print symbol. There is no need to switch out of Nemeth Code in order to braille the icon. The icon is listed on the Special Symbols page as a UEB symbol as follows.

Shapes Used as Signs of Omission

11.27 Spacing: When a sign of shape is used as a sign of omission or placeholder to represent a numeral, letter, sign of comparison, sign of operation, abbreviation, or any other item, the sign of shape is spaced in accordance with the rules for the omitted material it represents.

- 12 ÷ 4 = □ (a numeral is omitted—symbol is spaced from comparison sign)
 ⠠12 ⠨ ⠠4 ⠦ ⠠
- 40 dimes = \$ ○ (a numeral is omitted—symbol is unspaced from monetary symbol)
 ⠠40 ⠠dimes ⠦ ⠠\$ ⠠
- □ l = 1000 cc (a numeral is omitted—symbol is spaced from abbreviation "l")
 ⠠ ⠠l ⠦ ⠠1000 ⠠cc
- 15 ○ 15 = 30 (an operation sign is omitted—symbol is unspaced)
 ⠠15 ⠠ ⠠15 ⠦ ⠠30
- 24 hrs. = 1 △ (an abbreviation is omitted—symbol is spaced from preceding numeral)
 ⠠24 ⠠hrs. ⠦ ⠠ ⠠

Example 11.27-1 Fill in the square with the proper sign: $=$ or \neq .

$$15 \div 3 \square 3 \div 15$$


Figure 1: A 3D visualization of the 1000-dimensional feature space. The plot shows a dense cloud of points, with a central cluster of points and several smaller, more dispersed clusters. The axes are labeled with numerical values, indicating the high dimensionality of the data.





A sign of shape is unspaced from any braille indicator which applies to it.

- $\gg 24_{\diamond} + 11_{\diamond} = 40_5$ (numerals in subscript position are omitted)
 $\gg y^{\frac{1}{3}} = \sqrt[3]{\blacksquare}$ (radicand is omitted)





$$\gg \quad x \square y$$

1 yr \bigcirc 200 da

\gg ray ab  ray ac

 $15 \square 15 = 30$

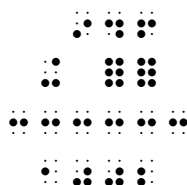
≫ 15 ○ 15 = 30





5/9/2020 revision

11.30 Omissions in Spatially-Arranged Problems: In a spatial arrangement, omissions are indicated with the general omission symbol regardless of the symbol used in print.

Example 11.30-1

$$\begin{array}{r}
 9 \ 4 \ 6 \\
 + \quad \square \ \square \\
 \hline
 1 \ 0 \ 0 \ 2
 \end{array}$$



In print, the omissions are indicated as two squares.

Instructions: Use the word "pencil" to name the icon shown below. After the completion of this practice drill, show how the icon will be listed on the Special Symbols page.

PRACTICE 11E

$$(2 * 3 + 9) \div 5 =$$

$$9 \cdot 35 \cdot y^x \cdot 17 \div =$$

$$212 \text{ } ^\circ \rightarrow ^\circ\text{C} \text{ End}$$

1. Fill in the box with the correct exponent.

a. $x^2 \times x^4 = x^{\square}$


b. $y^3 \times y^{\square} = y^9$

c. $z^{\square} \times z^5 = z^{15}$

Show your work with problems marked with .


A. $436 - \bigcirc = 102$

B. $5_8 + \bigcirc_8 = 22_8$

 C. $5 \frac{18}{12} = \square \frac{1}{2}$

D. Name two different operation signs that make this a true statement.

$$1 \square 1 = 1$$


 E. $\frac{15}{20} = \frac{3}{\square}$

Identified Signs of Shape

A sign of shape which is followed by a letter, a sequence of letters, or a numeral, is an *identified sign of shape*. The entire unit is mathematical and therefore brailled in Nemeth Code.

11.31 Spacing: There must be a space between the shape symbol and its identification. A space often does not appear in the print copy but it must be present in braille.

("angle theta")


Example 11.31-1  5 denotes "trapezoid 5."

The first 5 is associated with the mathematical shape and is included inside the switches.

A switch to Nemeth Code is not necessary for the second 5 – it is a freestanding numeral in UEB context.

11.31.1 Keep Together: A sign of shape and the letter, sequence of letters, or numeral which follows it is regarded as a single mathematical item and therefore should not be divided between braille lines.

Example 11.31-2 How many different triangles can you draw within the boundaries of  ABCD?  EFG?  HIJKLM?



11.31.2 Surrounding Symbols: The spacing before and after a sign of shape and its identification is subject to the spacing rules for the symbols preceding or following it.

$$\gg \triangle PQR \sim \triangle P'Q'R'$$

A space precedes and follows the tilde, which, in this case, is a sign of operation meaning "is similar to".






$$\gg \angle 2 + \angle 3 = \angle 4$$






Figure 1 consists of six sub-diagrams labeled (a) through (f), each showing a 3x3 grid of dots. In (a), 8 dots are present. In (b), 7 dots are present. In (c), 6 dots are present. In (d), 5 dots are present. In (e), 4 dots are present. In (f), 3 dots are present. The dots are arranged in a pattern that suggests a specific rule for their removal or movement over time.

There is no space before or after the operation sign (plus sign).





$$\gg A_{\triangle ABC} \quad \begin{array}{ccc} \bullet & \bullet & \bullet \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \bullet & \bullet & \bullet \end{array} \quad \begin{array}{ccc} \bullet & \bullet & \bullet \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \bullet & \bullet & \bullet \end{array}$$

11.33 A Shape Which Carries a Superscript or a Subscript: When a sign of shape carries a superscript, the level indicator is unspaced from the shape.

11.34 The English Letter Indicator: When an English letter, a Roman numeral, or a shortform letter combination identifies a shape, the English letter indicator is not used.

»	$\angle p$			("angle p")
»	\square ii			("square ii")

\gg \triangle abv ("triangle abv")

Example 11.34-1 \odot Q denotes "circle Q."

If such letters are in nonregular type, rules regarding typeform are followed and an English letter indicator is required if the variant typeform is retained.

Example 11.34-2 Compare $\bigcirc Z$ to $\bigcirc \mathbf{Z}$.

The figure consists of 10 small diagrams arranged in a single row, each showing a 2D grid of dots. The dots are black, and the background is white. The diagrams show a sequence of patterns that evolve from left to right. The patterns are composed of black dots on a white grid. The first diagram shows a small cluster of dots. As the sequence progresses, the cluster grows and changes shape, eventually forming a more complex, elongated structure by the 10th diagram.

If the sign of shape has a plural or a possessive ending, an English letter indicator may be required.

Example 11.34-3 Find the sum of \angle s a and b . Find the difference of \angle s acr and adr .

Figure 1: A 3x10 grid of 30 small plots showing the evolution of the system over time. The plots are arranged in three rows and ten columns. Each plot shows a 2D spatial distribution of points, representing the system's state at a specific time step. The points are colored red and blue, indicating different components of the system. The plots show a clear progression from left to right, with the system evolving from a simple initial state to a more complex, structured state.

Single letters "a" and "b" require an ELI when following Nemeth Code rules. (Review the definition of "single letter" in Lesson 4, section 4.10.) Letter combination "acr" requires an ELI because it is the same as a shortform; letter combination "adr" does not.

11.34.1 The Letter "m": Notation regarding angle measurement often uses the letter "m" for "measure". The letter "m" is brailled unspaced from the following symbol regardless of spacing used in the print copy.

\gg m $\angle \theta$ ⠠⠍⠗⠑⠒⠏⠶⠎⠨⠿⠠⠞⠊⠑⠗⠽⠤⠠⠭⠗⠁⠇⠑⠐⠆⠠⠞⠊⠑⠗⠽⠤⠠⠭⠗⠁⠇⠑⠐⠆ ("the measure of angle theta")

[illegible]

11.35 Use of the Numeric Indicator in an Enclosed List: The "enclosed list" was introduced in **Lesson 5** where it states that a numeric indicator is not used before a numeral in an enclosed list. More specifically, this rule applies to a numeral that occurs at the *beginning* of the item. A sign of shape and an identifying numeral which follows it are a single item even though a space occurs between them. In the context of an enclosed list, the numeric indicator is required for the identifying numeral because the numeral is not at the beginning of the item. Look carefully at the use and nonuse of the numeric indicator in each example below, as described in the comments.

$(\angle 1, \angle 2, \angle 3)$




In this enclosed list, each numeral needs a numeric indicator because it identifies the angle symbol—the numeral does not begin the item.

$\gg (\angle 1, 2\angle 1, 3\angle 1)$

Only the numerals which begin an item ("2" and "3") are brailled without a numeric indicator in this enclosed list.

The numerals ("1" and "2") begin each item in this enclosed list—a numeric indicator is not brailled. The letters ("a" and "b") are brailled without a letter indicator according to the rules governing identified signs of shape.

PRACTICE 11F

1.  ABCD is a square.  EFGH is a parallelogram.  JKLM is a rhombus.
2. Compare triangles: $\triangle ADM \cong \triangle A'D'M'$. $\triangle BEP \not\cong \triangle CFP$.
3. Should $\triangle ABV$ be included in the set $\{\triangle 3, \angle GHA, \diamond 2\}$?
4. $\angle 3 + \angle 4 = 90^\circ$
5. $m\angle p + m\angle q = 180^\circ$
6. $m^\circ \angle \theta = -45$
7. $A_{\triangle DEF} = \frac{1}{2}bh$
8. $\angle ECB = \frac{1}{2}\angle ABC$

Displayed Material with Labels

11.36 Recognition: Displayed mathematical expressions may be labeled in print with a unique number or letter printed in a location that is visually conspicuous, often in the right margin. That label is then used in place of the actual expression later in an example or in the narrative. This allows for compact presentation of a problem.

Example 11.36-1

$$a \times b = b \times a. \quad (2)$$

Line 6: Same comment as line 3. Note that the labels are bold in print but the typeform is disregarded in braille.




























Example 10.36-2

Figure 1 displays a set of 22 dot patterns arranged in two rows of 12. The top row contains patterns for digits 0 through 9, and the bottom row contains patterns for digits 10 through 21. Each pattern is a 4x4 grid of dots, where the presence or absence of a dot at a specific position represents a binary value (0 or 1) for that digit.

Example 11.37-1

Figure 1 shows a 2x10 grid of dot patterns. The top row contains 10 patterns, and the bottom row contains 10 patterns. Each pattern is a 3x3 grid of dots, with some dots missing to form various shapes. The patterns are arranged in a sequence that suggests a visual search task.

Example 11.37-2

1                           

Lines 2-3: Displayed margins to itemized material, (5-7)

Figure 10: A sequence of 18 diagrams illustrating the steps of the algorithm. Each diagram shows a grid of dots representing a state. The sequence shows the evolution of the state from left to right, with the final state being a single dot in the top-left corner.

Since the location of the citation is not changed from its location in print, a transcriber's note is not needed.

PRACTICE 11G

$$ax^2 + bx + c = 0 \quad (1)$$
$$a^2 + b^2 = c^2 \quad (2)$$

5/9/2020 revision

Labeled Mathematical Statements

Definition A set which can be put into one-to-one correspondence with the natural numbers is called a countable set.

11.38.3 Spacing and Margins: A line is left blank before the beginning and after the end of the entire labeled statement. Normal paragraphing (3-1) is applied, with the label beginning the paragraph.

Definition A set which can be put into one-to-one correspondence with the natural numbers is called a countable set.

In print, the label "Definition" is a marginal heading. Only the first letter is capitalized and the word is in boldface. In braille, typeface of the label is disregarded, the label is fully capitalized and is placed as a paragraph heading beginning in cell 3. The definition is printed entirely in boldface. Uniform typeface is disregarded in braille. A blank line precedes and follows the labeled statement.

A labeled statement may begin on line 1 of the braille page.

Example 11.38-2 **Theorem 4.** *The diagonals of a rectangle are equal.*

1

2

(blank line)

In print, "Theorem 4" is bold and the statement is in italics.

A labeled statement may end on line 25 of the braille page.

23 (blank line)

24 

25 

If the statement is printed in a box, follow *Braille Formats* guidelines regarding blank lines.

Example 11.38-3

Bauer–Fike Theorem. Let μ be an eigenvalue of $A + \delta A$. Then there exists $\lambda \in \Lambda(A)$ such that

$$|\lambda - \mu| \leq \kappa_p(V) \|\delta A\|_p .$$

(blank line)

The image displays a 6x40 grid of dots. The top and bottom rows are solid black. The four middle rows contain a complex arrangement of dots that form various symbols and shapes. These include horizontal bars, vertical bars, and more intricate patterns that resemble stylized letters or abstract figures. The overall effect is a dense, textured composition where the white space between the dots creates the primary visual elements.

(blank line)

The labeled statement is boxed. Box lines are retained in braille for distinction. The label "Bauer-Fike Theorem." is printed as a paragraph heading. Only the initial letters are capitalized and the label is in boldface. In braille, typeface is disregarded and the label is fully capitalized. The definition itself is printed in normal typeface, with the exception of the letters in the mathematical expressions which are in italics. In braille, italics applied to a variable are disregarded.

Review unfamiliar symbols. This example above includes Greek letters mu, delta, lambda (both lowercase and uppercase), and kappa as well as the comparison sign for

*"membership". You can assume the letter A is the English letter, not a Greek Alpha. Several uppercase Greek letters are generally not used as math symbols because they look identical to certain uppercase Latin (English) letters. Review the Greek Alphabet Table in **Lesson 5**.*

11.39 Significant Typeface: If, in the body of the labeled statement, a word or phrase is singled out for special attention by using a non-regular typeface (for the purpose of definition or other elaboration), the change in typeface is retained in braille. Use the appropriate UEB or Nemeth Code typeface indicators. UEB indicators are used outside of the code switches; Nemeth Code indicators are used inside the code switches.

Analysis: In the next example, the label "Definition." is printed in boldface. Only the first letter is capitalized. In braille, typeface is disregarded and, instead, the label is fully capitalized. The statement is printed entirely in italics but two words are emphasized in bold italics. In braille, the superfluous typeface (italics) is disregarded but the typeface of the emphasized words (boldface) is retained.

Example 11.39-1 **Definition.** A polygon that has *five* sides is a **pentagon**.

(blank line)

(blank line)

Recall from **Lesson 7** that a switch from UEB to Nemeth Code terminates the effect of a UEB typeform indicator.

Analysis: In the next example, the label "Definition" is printed in italics and only the first letter is capitalized. In braille, the label is fully capitalized. The statement is printed entirely in boldface. This superfluous typeface is ignored in braille. One phrase is emphasized by underlining. The underlining is retained in braille.

Example 11.39-2 **Definition** $x + yi = a + bi$ if and only if $x = a$ and $y = b$.

(blank line)

Figure 1 shows a 2x10 grid of Braille characters. The top row contains 10 characters, and the bottom row contains 10 characters. Each character is a 2x3 grid of dots, with some dots filled in black to represent the Braille character.

(blank line)

The underlining of the passage is implicitly terminated by the switch to Nemeth Code.

Implicit termination does not apply to capitalization. A fully capitalized passage must be explicitly terminated.

Example 11.39-3 **Definition** $x + yi = a + bi$ IF AND ONLY IF $x = a$ and $y = b$.

(blank line)

(blank line)

PRACTICE 11H

Labeled Mathematical Statements

Pythagorean Theorem *In a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.*

$$c^2 = a^2 + b^2$$

<p>DEFINITION A positive number expressed in the form: $a \times 10^n$, where $1 \leq a < 10$ and n is an integer is said to be written in scientific notation.</p>
--

Typeform Indicators for Mathematical Words and Phrases

11.40 Italic and Boldface Typeform Indicators: When significant typeform is retained inside of the Nemeth Code switches, Nemeth Code typeform indicators are used. **Lesson 7** introduced the Nemeth Code typeform indicators for letters, numerals, symbols, and compound expressions. When typeform is retained for a mathematical *word or phrase*, the following rules apply.

11.40.1 One Word in Italics or Boldface

For One Word	
Italic Typeform Indicator	⋮
Opening Boldface Type Indicator	⋮ ⋮ ⋮
Closing Boldface Type Indicator	⋮ ⋮ ⋮

The one-cell italic typeform indicator is unspaced from the following word.


four


Example 11.40-1 The subset of even-number words is shown in italics.

{one, *two*, three, *four*, five}

Figure 1: A 2D grid of 10x10 cells, each containing a 3x3 sub-grid of dots. The dots are arranged in a pattern that forms a larger grid of 10x10 cells, with each cell containing a 3x3 sub-grid of dots. The dots are arranged in a pattern that forms a larger grid of 10x10 cells, with each cell containing a 3x3 sub-grid of dots.

The three-cell boldface type indicators are preceded and followed by a space and must not stand alone on a line.


 four
 



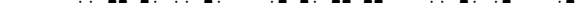

Example 11.40-2 In this set, the even-number word is shown in boldface.

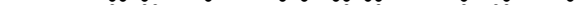
{three, **four**, five}

*Note: The one-cell boldface typeform indicator of the Nemeth Code **⠠** is applied to a word only in the context of a compound expression. See **Lesson 7**.*

$\geq \frac{9}{100}$

$\geq 9\%$

$\gg P(A \text{ and } B) = 0$


$\gg P(A \text{ or } B) = ?$


5/9/2020 revision

11.40.2 A Phrase Italics or Boldface

For a Phrase	
Opening Italic Type Indicator	⠠ ⠦ ⠨
Closing Italic Type Indicator	⠨ ⠦ ⠠
Opening Boldface Type Indicator	⠠ ⠦ ⠨
Closing Boldface Type Indicator	⠨ ⠦ ⠠

The three-cell typeform indicators are preceded and followed by a space and must not stand alone on a line. When both indicators are required for the same word or phrase, they are unspaced from each other and are closed in the opposite order as opened.

4.9 sq. ft.

Assume the italics is significant in this illustration.

11.41 Code Switching Within an Emphasized Passage: If code switching is necessary within an emphasized technical passage, the beginning typeform indicators are repeated after each switch to show that emphasis continues. Switching from Nemeth Code to UEB does not implicitly terminate a Nemeth Code typeform – the appropriate closing typeform indicator must be brailled before terminating Nemeth Code.

Example 11.41-1 If the cost **after applying the 15% discount** is \$25.34, what is the original price?

Figure 1: A 3D visualization of the proposed model architecture. The diagram illustrates the flow of information from input data (represented by a grid of points) through a series of processing layers (represented by colored blocks) to the final output (represented by a grid of points). The layers are labeled with mathematical symbols and indices, indicating the hierarchical structure of the model.

It is first determined that the boldface should be retained because its purpose here is to focus attention on the phrase.

Line 1: UEB boldface passage indicator applies to three words. The switch from UEB to Nemeth Code terminates the effect of the UEB typeform indicator without the need for a UEB termination indicator.

Line 2: The boldface indicator of the Nemeth Code is used for the boldfaced mathematical item, 15%. The Nemeth Code closing boldface indicator is required before switching out of Nemeth Code.

Line 2: The nonregular typeform continues after the termination of the mathematical portion, so a UEB typeform indicator must be re-entered.

For further practice, see Appendix A—Reading Practice.

ANSWERS TO PRACTICE MATERIAL

The first opening Nemeth Code indicator may also be placed at the beginning of the series of shapes on line 4.

Math displayed to a 3-1 narrative paragraph begins in cell 3.

Math displayed to a 3-1 narrative paragraph begins in cell 3.

This is three paragraphs. Math displayed to a 3-1 narrative paragraph begins in cell 3.

Math displayed to a 3-1 narrative paragraph begins in cell 3.

Math displayed to a 3-1 narrative paragraph begins in cell 3.

Math displayed to a 3-1 narrative paragraph begins in cell 3.

Math displayed to a 3-1 narrative paragraph begins in cell 3.

The image displays a 10x10 grid of 100 small 3x3 dot patterns. Each pattern consists of a 3x3 grid of dots, where some dots are black (active) and others are white (inactive). The patterns are arranged in rows and columns, showing various combinations of active and inactive dots. The patterns are arranged in a way that suggests a sequence or a specific arrangement, but they do not form a recognizable image or text.

Exercise 11 will be available when this course is finished being written and is no longer "Provisional".

11-45